

Isleham Primary School

**Calculation Policy** 

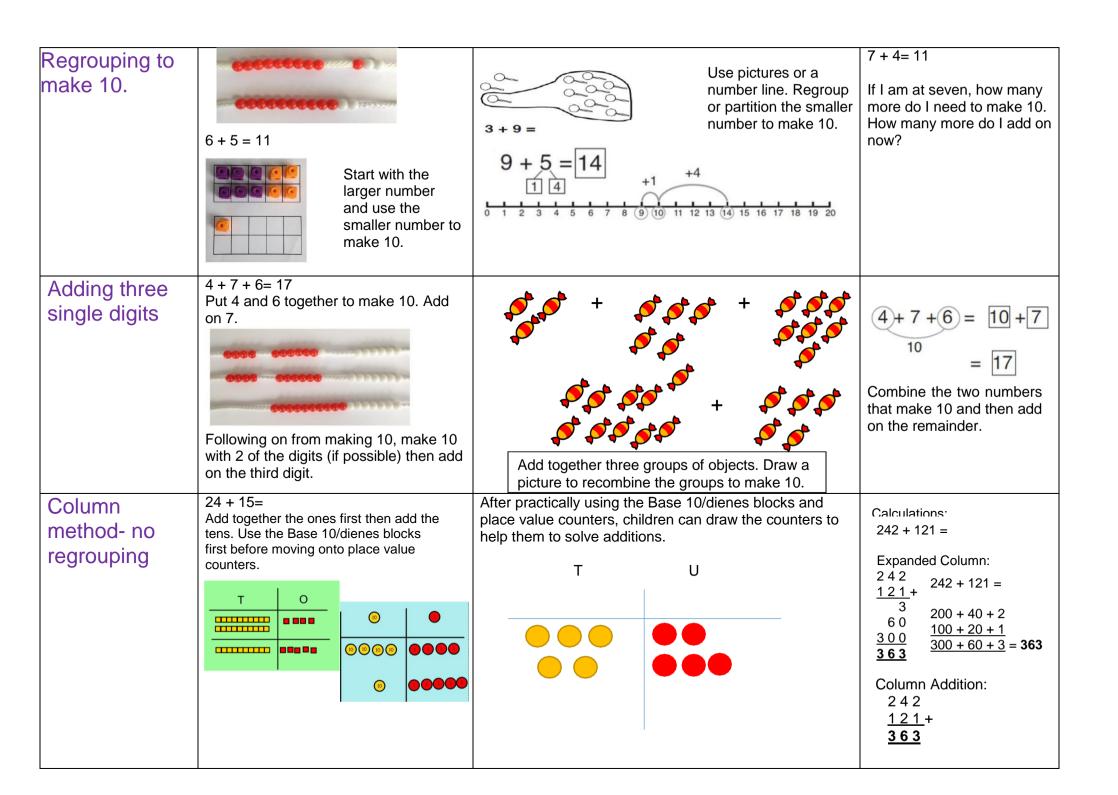
Progress in Calculation EYFS to Year 6

Addition
Subtraction
Multiplication
Division

#### Progression in Calculations

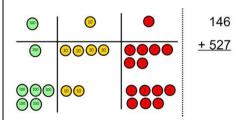
#### **Addition**

| Objective and Strategies                                   | Concrete   | Pictorial  | Abstract   |
|--|--|--|--|
| Combining two parts to make a whole: part-part whole model | Use cubes to add two numbers together as a group or in a bar.  | Use pictures to add two numbers together as a group or in a bar.   | 4 + 3 = 7  10= 6 + 4  Use the part-part whole diagram as shown above to move into the abstract.        |
| Starting at the larger number and counting on              | Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer. | 12 + 5 = 17  Start at the larger number on the number line and count on in ones or in one jump to find the answer. | 5 + 12 = 17  Place the larger number in your head and count on the smaller number to find your answer. |

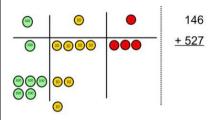


#### Column methodregrouping

Make both numbers on a place value grid.



Add up the ones and exchange 10 ones for one 10.

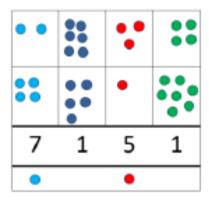


Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10/dienes blocks to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.



Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

Expanded column addition

$$358 + 473 =$$

$$358 + 473 =$$

$$\frac{+473}{11} = 300 + 50 + 8$$

$$\frac{400 + 70 + 3}{700 + 120 + 11} = 831$$

$$\frac{700}{831}$$

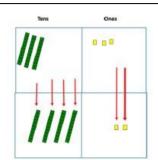
As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here too.

#### **Subtraction**

| Objective and Strategies | Concrete  | Pictorial  | Abstract   |
|--------------------------|---|--|--|
| Taking away ones         | Use physical objects, counters, cubes etc to show how objects can be taken away.                                  | Cross out drawn objects to show what has been taken away.  | 18 - 3= 15   |
|                          | 6-2=4   | $     \begin{array}{cccc}                                  $                                       | 8 - 2 = 6  |
| Counting back            | Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. | Count back on a number line or number track  9 10 11 12 13 14 15                                   | Put 13 in your head, count back 4. What number are you at? Use your fingers to help. |
|                          | 13 – 4  | Start at the bigger number and count back the smaller number showing the jumps on the number line. |  |
|                          | Use counters and move them away from the group as you take them away counting backwards as you go.                | -10<br>-1 -1 -1  |  |
|                          |   | This can progress all the way to counting back using two 2 digit numbers.                          |  |

| Find the    | Compare amounts and objects to find     |  | Hannah has 23 sandwiches,    |
|-------------|---|--|------------------------------|
|             | the difference.                         | +6 Count on to   | Helen has 15 sandwiches.     |
| difference  | and amoroned.                           | find the   | Find the difference between  |
|             |   | difference.  | the number of sandwiches.    |
|             | Use cubes to                            | difference.  | the number of sandwiches.    |
|             |   | 0 1 2 3 4 5 6 7 8 9 10 11 12                                   |                              |
|             | build towers or                         |  |                              |
|             | make bars to                            |  |                              |
|             | find the                                | Comparison Bar Models  |                              |
|             | difference                              | 5  |                              |
|             | 5 Pencils                               | Draw bars to Lisa is 13 years old. Her sister is 22 years old. |                              |
|             | Use basic bar                           | find Find the difference in age between them.                  |                              |
|             | models with                             | the difference 13 ?  |                              |
|             | items to find                           | between 2  |                              |
|             | the difference                          | numbers.   |                              |
|             | 3 Erasers 7                             |  |                              |
|             |   | 22   |                              |
|             |   |  |                              |
|             |   |  |                              |
| Part-Part   | Link to addition- use                   | Use a pictorial representation of objects to show the          |                              |
| Whole Model | the part whole model                    | part-part whole model.   | 5                            |
| whole woder | to help explain the                     |  |                              |
|             | inverse between                         |  | 10                           |
|             | addition and                            |  |                              |
|             | subtraction.                            |  |                              |
|             |   |  |                              |
|             | If 10 is the whole and 6 is one of the  |  | Move to using numbers        |
|             | parts. What is the other part?          |  | within the part whole model. |
|             |   |  | Missing number questions.    |
|             | 10 - 6 =                                |  |                              |
| Make 10     | 14 – 9 =                                |  |                              |
| mano 10     |   | 13 - 7 = 6   | 16 – 8=                      |
|             | 000000000000000000000000000000000000000 | 13 - 7 = 6 -4 -3   |                              |
|             |   | 34   | How many do we take off to   |
|             |   | 0 1 2 3 4 5 (6) 7 8 9 (10) 11 12 (13) 14 15 16 17 18 19 20     | reach the next 10?           |
|             |   | Start at 13. Take away 3 to reach 10. Then take away the       |                              |
|             | Make 14 on the ten frame. Take sweet    | remaining 4 so you have taken away 7 altogether. You           | How many do we have left     |
|             | Make 14 on the ten frame. Take away     | have reached your answer.                                      | to take off?                 |
|             | the four first to make 10 and then      | nave reached your answer.                                      |                              |
|             | takeaway one more so you have taken     |  |                              |
|             | away 5. You are left with the answer of |  |                              |
|             | 9.                                      |  |                              |

#### Column method without regrouping



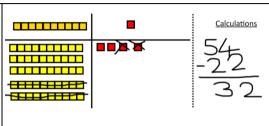
Show how you partition

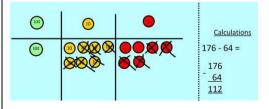
numbers to

subtract.
Again make
the larger
number first

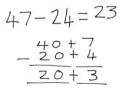
Use Base 10/dienes to make the larger number then take the smaller number away.

36-14=22 T u 30 30 - 10 - 30 10 - 20





Draw the Base 10 or place value counters alongside the written calculation to help show the working out and thought processes.



This will lead to a clear written column subtraction.



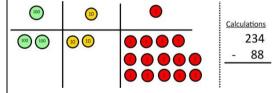
## Column method with regrouping

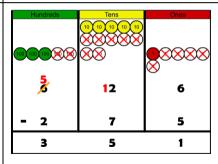
Use Base 10/dienes to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

Make the larger number with the place value counters

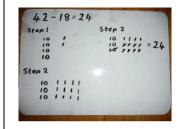
| 100     | 10          | • | Calculations       |
|---------|-------------|---|--------------------|
| 100 100 | (1) (1) (1) |   | 234<br><u>- 88</u> |

Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.





Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.



When confident, children can find their own way to record the exchange/regrouping.

Just writing the numbers as shown here shows that the child understands the method

and knows when to exchange/regroup.

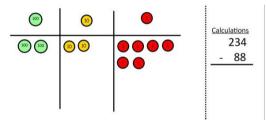


Children can start their formal written method by partitioning the number into clear place value columns.

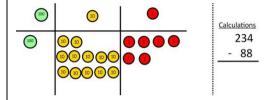


Moving forward the children use a more compact method. It is vital that this next step is only made once the children have a solid and secure place value understanding.

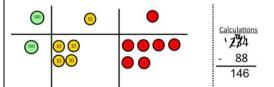
Now I can subtract my ones.



Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Now I can take away eight tens and complete my subtraction



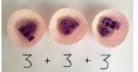
Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

This will lead to an understanding of subtracting any number including decimals.

#### **Multiplication**

| Objective and Strategies | Concrete   | Pictorial   | Abstract   |
|--------------------------|--|---|--|
| Doubling                 | Use practical activities to show how to double a number.   | Draw pictures to show how to double a number.  Double 4 is 8                | 16 10 6 10 x2 20 12 Partition a number and then                                |
| Counting in              | 4×2=8  |   | double each part before recombining it back together.  Count in multiples of a |
| multiples                | and the second state of th | Sur Sur Sur Sur Sur Sur   | number aloud.  Write sequences with multiples of numbers.                      |
|                          | Counting in multiples supported by concrete objects in equal groups.   | Use a number line or pictures to continue support in                        | 2, 4, 6, 8, 10<br>5, 10, 15, 20, 25, 30  |
|                          |  | Use a number line or pictures to continue support in counting in multiples. |  |

### Repeated addition





Use different objects to add equal groups.

There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?

2 add 2 add 2 equals 6







5 + 5 + 5 = 15

Write addition sentences to describe objects and pictures.



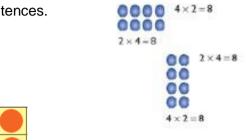
Arraysshowing commutative multiplication Create arrays using counters/ cubes to show multiplication sentences.





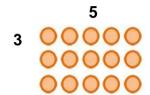
Draw arrays in different rotations to find **commutative** multiplication sentences.

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15



Link arrays to area of rectangles.

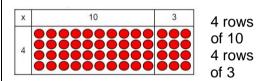
Use an array to write multiplication sentences and reinforce repeated addition.



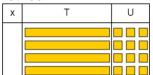
$$3 + 3 + 3 + 3 + 3 + 3 = 15$$
  
 $5 + 5 + 5 = 15$ 

#### **Grid Method**

Show the link with arrays to first introduce the grid method.



Move on to using Base 10/dienes to move towards a more compact method.

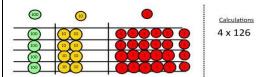


4 rows of 13

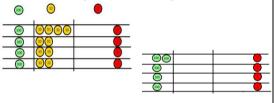
Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.



Fill each row with 126.

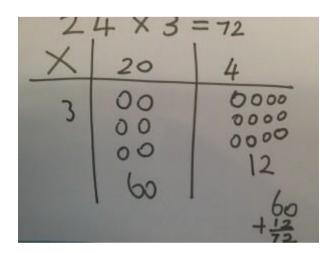


Add up each column, starting with the ones making any exchanges needed.



Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

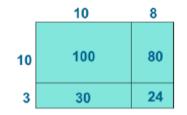


Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

| × | 30  | 5  |
|---|-----|----|
| 7 | 210 | 35 |

$$210 + 35 = 245$$

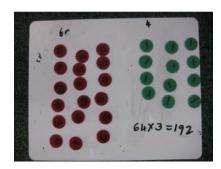
Moving forward, multiply by a 2 digit number showing the different rows within the grid method.



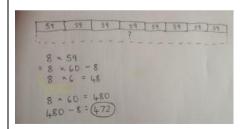
| Х  | 1000  | 300  | 40  | 2  |
|----|-------|------|-----|----|
| 10 | 10000 | 3000 | 400 | 20 |
| 8  | 8000  | 2400 | 320 | 16 |

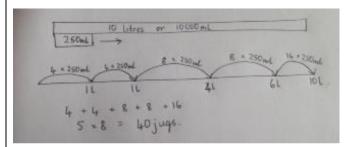
## Column multiplication

Children can continue to be supported by place value counters at the stage of multiplication.



It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below. Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.





Start with long multiplication, reminding the children about lining up their numbers clearly in columns.

If it helps, children can write out what they are solving next to their answer.

This moves to the more compact method.

#### **Division**

| Objective and Strategies    | Concrete   | Pictorial   | Abstract   |
|-----------------------------|--|---|--|
| Sharing objects into groups | I have 10 cubes, can you share them equally in 2 groups?   | Children use pictures or shapes to share quantities. $8 \div 2 = 4$   | Share 9 buns between three people. $9 \div 3 = 3$  |
| Division as grouping        | Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.  96 ÷ 3 = 32 | Use a <b>number line</b> to show jumps in groups. The number of jumps equals the number of groups.  Think of the <b>bar as a whole</b> . Split it into the number of groups you are dividing by and work out how many would be within each group.  Manipulation of the empty number line:  16 ÷ 8 = 2  Manipulation of the empty number line:  16 ÷ 7 =  7x10=70  7x10=70  7x10=70  7x8=56  0  196 ÷ 7 = 28 | 28 ÷ 7 = 4  Divide 28 into 7 groups. How many are in each group?  196 ÷ 7 = 28  I have 196 pencils and I need to share them between the 7 classes in the school. How many pencils does each class get? |

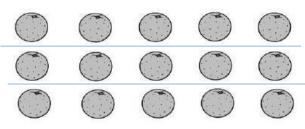
# Division within arravs Division with a remainder

Link division to multiplication by creating an array and thinking about the number



sentences that can be created.

Eg 
$$15 \div 3 = 5$$
  $5 \times 3 = 15$   
 $15 \div 5 = 3$   $3 \times 5 = 15$ 



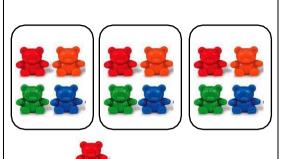
Draw an array and use lines to split the array into groups to make multiplication and division sentences.

Find the inverse of multiplication and division sentences by creating four linking number sentences.

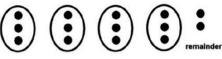
$$7 \times 4 = 28$$
  
 $4 \times 7 = 28$   
 $28 \div 7 = 4$   
 $28 \div 4 = 7$ 

14 ÷ 3 =

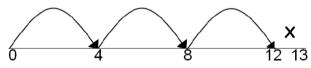
Divide objects between groups and see how much is left over

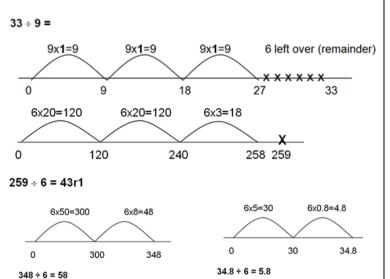


Draw dots and group them to divide an amount and clearly show a remainder.



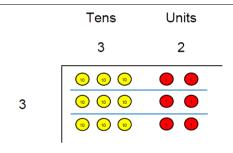
Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



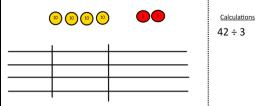


Complete written divisions and show the remainder using r.

#### Short division

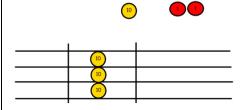


Use place value counters to divide using the bus stop method alongside

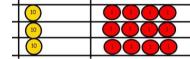


42 ÷ 3=

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.

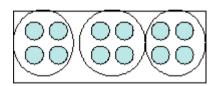


We exchange this ten for ten ones and then share the ones equally among the groups.



We look how much in 1 group so the answer is 14.

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

These methods should be re-modelled on the empty number line to ensure a secure understanding.

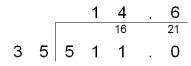
#### Short division

...and with remainders:

Begin with division calculations that divide equally with no remainder.

Move onto divisions with a remainder.

Finally move into decimal places to divide the total accurately.



Short division, for dividing by a single digit: e.g. 6497 ÷ 8

0812·125 8)64917·000 Short division with remainders: Pupils should continue to use this method, but with numbers to at least 4 digits, and understand how to express remainders as fractions, decimals, whole number remainders, or rounded numbers. Real life problem solving contexts need to be the starting point, where pupils have to consider the most appropriate way to

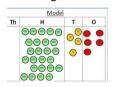
Calculating a decimal remainder: In this example, rather than expressing the remainder as <u>r.1</u>, a decimal point is added after the units because there is still a remainder, and the one remainder is carried onto zeros after the decimal point (to show there was no decimal value in the original number). Keep dividing to an appropriate degree of accuracy for the problem being solved.

#### Long division

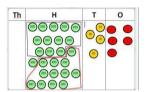


2544 ÷ 12 How many groups of 12 thousands do we have? None

Exchange 2 thousand for 20 hundreds.

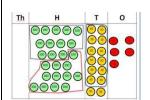


How many groups of 12 are in 25 hundreds? 2 groups. Circle them. We have grouped 24 hundreds so can take them off and we are left with one.



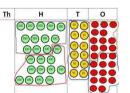
$$\begin{array}{r}
 02 \\
 \hline
 12 2544 \\
 \underline{24} \\
 1
 \end{array}$$

Exchange the one hundred for ten tens so now we have 14 tens. How many groups of 12 are in 14? 1 remainder 2



$$\begin{array}{r}
0 2 1 \\
12 2544 \\
\underline{24} \\
14 \\
\underline{12} \\
2
\end{array}$$

Exchange the two tens for twenty ones so now we have 24 ones. How many groups of 12 are in 24? 2



Instead of using physical counters, students can draw the counters and circle the groups on a whiteboard or in their books.

Use this method to explain what is happening and as soon as they have understood, move on to the abstract method as this can be **a time consuming process.** 

#### Chunking method for division

As children begin to use their knowledge of multiplication tables, particularly with multiples of ten for each table, they can progress from taking 10 chunks of a divisor to  $30 \times 6 = 180$  and subtract this larger chunk.

432 ÷ 15 becomes

Answer: 28 remainder 12

432 ÷ 15 becomes

Answer: 28 4